

Laboratory 8 – Bebop to the Boolean Boogie***A: /3 B: /4 C: /8 + 5 bonus****Goal:**

This lab is split in three parts of increasing difficulty:

A) (Somewhat difficult)

We will learn a simple technique to store n bits of data into an n bit memory given a single serial input line to the memory. We will work with $n=4$

B) (More difficult, though not too much if you have understood Part A)

We will use the technique developed in part A to make the numbers ‘dance’ around (hence the title of the assignment) – this can be used to create blinking lights like those used on festive occasions

C) (Very difficult)

We will enhance the technique of Part B to a non-trivial level – and demonstrate how to make the numbers dance around in a random manner to create a sequence of 4 bit (pseudo)random numbers

Part A: Storage of n bits

Recall from earlier exercises that the reliable storage of one data bit requires the use of one D register.

Design a memory circuit that is able to store $n=4$ bits of data $D_3D_2D_1D_0$ with the following constraints:

1. The circuit is driven by a clock signal.
2. The input to your circuit is a *single* serial line. At every clock cycle $i = 0,1,2,3$ the values of the data bits $D_0 D_1 D_2 D_3$ (in that order) are made available on the input.

Draw your circuit design here:

Build your design with the 74LS175 4-bit D register IC. It is useful to connect an LED+220 Ω at the output of each D-register to clearly indicate the status of the bit.

Demonstrate its operation by using the 1 Hz clock and sending in a simple input like 10001 using the push button switch on the logic signal generator. Note that after the 4th clock input, your memory will start getting overwritten!

A: /3

Part B: Make n bits perform a rhythmic dance

Recall the use of decorative lights in recent festivities – they typically have a string of lights with the on/off states alternating in time to give an illusion of motion along the length of the lights.

Modify your circuit of Part B, to make such a dancing light pattern that repeats itself long as the clock signal is sent in.

Hints:

- 1) 'Repetition' usually equates to some type of feedback
- 2) Each D register in the 4-bit 74LS175 has both a Q and Q-bar output
- 3) You can make a 4-bit lighting string for Ganesh Chaturthi by re-arranging one of the inputs & outputs in the design of Part A.
- 4) Only one extra connection is needed over the design of Part A
- 5) The D-register IC has a global reset pin $\overline{\text{CLR}}$. When it is connected to logic 0, all bits are cleared to 0.

Draw the (re)-design of your circuit here. Modify the connections of Part A on the breadboard to demonstrate its operation

Part C: Make n bits dance randomly

In Part B, the circuit was setup to repeat the same sequence of bits.

Inserting a *linear* operation in the repetitive loop can *change* the sequence of bits that is repeated.

Two such linear operations are $A(X\text{-NOR})B$ or $A(XOR)B$ which are very much like algebraic multiplication: $A(X\text{-NOR})B = \text{NOT}[A(XOR)B] = 1$ only for $A=B=0$ and $A=B=1$; 0 if $A \neq B$.

- 1) The objective of Part C is that at every clock cycle the sequence of bits $D_3D_2D_1D_0$ must be random
- 2) This can be done by using the original design of Part A, with the concept of repetitive feedback used in Part B.
- 3) The feedback must be modified by inserting a linear operation in the path. Tap two suitable bits D_A and D_B from the 4-bit memory and insert the $D_A(X\text{-NOR})D_B$ operation in the feedback path.

C:	/3 : Basic design
	/5 : Choice of $D_A D_B$
	/5 : Proof of randomness

Circuit Design for Part C here:

3 marks

Note: Initially you can choose by trial and error which points 'A' and 'B' to tap as D_A and D_B from $D_3D_2D_1D_0$. You must demonstrate that the sequence of numbers $D_3D_2D_1D_0$ on successive clock pulses at least *looks* random i.e. it does not get stuck at some fixed number which repeats forever.

-Demo -

5 marks

For those with a mathematical and/or Boolean inclination for BeBop:

For an arbitrary value of n bits calculate how long a sequence of random numbers $D_nD_{n-1}...D_0$ such a design would go through before repeating itself. (It's easy to work this out explicitly with $n=3$)

The general formula is quite simple, though its derivation may require a little bit of work.

It leads to the fact that, for example, a 32-bit memory register with a single linear operation in the feedback can create a sequence of 4,294,967,295 random combinations before repeating.

5 marks (and probably a couple of extra pages!)

Name:

Roll #
